| Your Name:  |                       |  |
|-------------|-----------------------|--|
| Names of pe | ople you worked with: |  |

**Task**: Consider a setting where we are interested in comparing the soda preference across three of the Claremont Colleges. [Ask yourself what the observational units and variables are for the study below!] The following incomplete table describes the soda preferences for a sample of Pomona, Pitzer, and CMC students.

|         | Soda  | Preference |        |       |
|---------|-------|------------|--------|-------|
| College | Pepsi | Root beer  | Sprite | Total |
| CMC     |       |            |        | 36    |
| Pitzer  |       |            |        | 24    |
| Pomona  |       |            |        | 60    |
| Total   | 40    | 60         | 20     | 120   |

- 1. Fill in the table as if College and Soda Preference are independent variables. Note that half of the students prefer root beer. So, how many of the Pitzer students would you expect to prefer root beer? You are calculating the value of the data that you would **expect** under the null hypothesis.
- 2. Let's say the actual data (i.e., the **observed** data) is given by the following table. Create a new 3x3 table where each entry represents the difference (i.e., subtraction) between the observed value and the expected value (expected value is given in #1).

|         | Soda  | Preference |        |       |
|---------|-------|------------|--------|-------|
| College | Pepsi | Root beer  | Sprite | Total |
| CMC     | 10    | 17         | 9      | 36    |
| Pitzer  | 6     | 16         | 2      | 24    |
| Pomona  | 24    | 27         | 9      | 60    |
| Total   | 40    | 60         | 20     | 120   |

3. Fill out the full 3x3 table one last time with each of the 9 entries as:

$$\frac{(Observed-Expected)^2}{Expected}.$$

## Solution:

## $1.\ Expected$

|         | Soda  | Preference |        |       |
|---------|-------|------------|--------|-------|
| College | Pepsi | Root beer  | Sprite | Total |
| CMC     | 12    | 18         | 6      | 36    |
| Pitzer  | 8     | 12         | 4      | 24    |
| Pomona  | 20    | 30         | 10     | 60    |
| Total   | 40    | 60         | 20     | 120   |

## $2. \ Observed-Expected$

|         | Soda  | Preference |        |       |
|---------|-------|------------|--------|-------|
| College | Pepsi | Root beer  | Sprite | Total |
| CMC     | -2    | -1         | 3      | 0     |
| Pitzer  | -2    | +4         | -2     | 0     |
| Pomona  | +4    | -3         | -1     | 0     |
| Total   | 0     | 0          | 0      |       |

## $3. \ (Observed-Expected)^2/Expected$

| C-11    | Soda  | Preference | C t -  |
|---------|-------|------------|--------|
| College | Pepsi | Root beer  | Sprite |
| CMC     | 0.33  | 0.06       | 1.5    |
| Pitzer  | 0.5   | 1.3        | 1.0    |
| Pomona  | 0.8   | 0.3        | 0.1    |