WU #11 - Math 58B, Spring 2023

Tuesday, Feb 21, 2023

Your Name:

Names of people you worked with:

- 1. Mountains or beach?
- 2. What is the difference between a Z score and Z^* ?
- 3. You are trying to convince your college to offer more vegetarian options at mealtime, and you believe that 40% of students are vegetarians. The college says they disagree, and they won't change the offerings unless you can convince them that more than 35% of the student body is vegetarian.

Let's say it is a one sided test with level of significance of 0.1. Also, assume that the sample size will be big enough so that the central limit theorem holds. Start by suggesting a sample size of 50 people.

- a. What are the null and alternative hypotheses?
- b. What is the formula for the Z-score which will assess whether or not you reject H_0 ?
- c. What is the Z^* value above which you will reject H_0 ? (If you draw the picture, I'll tell you the number.)
- d. What \hat{p} do you need to get to reject H_0 (with n = 50)?
- e. If, in fact, the true proportion of vegetarians is p = 0.4, what is the probability that you will reject? (Again, if you can draw the correct picture, I'll tell you the number.)
- f. What is your power?
- g. What would you do here to increase your power? Is your solution always feasible in other experiments?

Solution:

a. $H_0: p = 0.35, H_a: p > 0.35$ b.

$$Z = \frac{\hat{p} - p}{\sqrt{p \cdot (1 - p)/n}} = \frac{\hat{p} - 0.35}{\sqrt{0.35 \cdot 0.65/50}}$$

c.

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xqnorm(0.9, mean = 0, sd = 1)
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If X ~ N(0, 1), then
P(X <= 1.281552) = 0.9
P(X > 1.281552) = 0.1
##



[1] 0.3016659

- f. With 50 observations, there is only a 0.3 probability (power) that the random sample would reject H_0 even if 40% of students were truly vegetarians.
- g. To get to a higher power, more observations need to be sampled. That isn't always possible because often collecting data is expensive and time consuming.

Questions you should be able to answer:

- Why is p used in the denominator of the Z-score (instead of \hat{p})?
- Why is p = 0.35 instead of p = 0.4 in H_0 ?
- Why is the alternative direction > instead of < ?
- Why is the xpnorm() in part (e) centered at 0.4 with a SD of $\sqrt{0.4 \cdot 0.6/50}$?
- Is power always positively related to sample size? Why?